

# DECAY MODES AND A LIMIT OF EXISTENCE OF NUCLEI

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# How is the limit of elements?

## Chemistry

1	2											13	14	15	16	17	18		
1	H											He							
2	Li	Be											B	C	N	O	F	Ne	
3	Na	Mg											Al	Si	P	S	Cl	Ar	
4	K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr	
5	Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe	
6	Cs	Ba	La*	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At	Rn	
7	Fr	Ra	Ac**	Rf	Db	Sg	Bh	Hs	Mt	Ds	Rg	Cn	113	114	115	116	117	118	
		(119)(120)		Sa***		(156)	(157)	(158)	(159)	(160)	(161)	(162)	(163)	(164)					
		(167)(168)												(167)	(168)	(169)	(170)	(171)	(172)

- In chemical study, elements up to Z~172 have been discussed.
- Are such elements can be existed?
- In other words, does the corresponding nuclei exist in certain half-lives?

## New elements? How far?

La*	Lanthanides	La	Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu
Ac**	Actinides	Ac	Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr
Sa***	Superactinides	(121)	(122)	(123)	(124)	(125)	(126)	(127)	...	...	...	(151)	(152)	(153)	(154)	(155)

P. Pyykko presented a more improved table.

# How far does the area of nuclei extend? -some qualitative estimations-

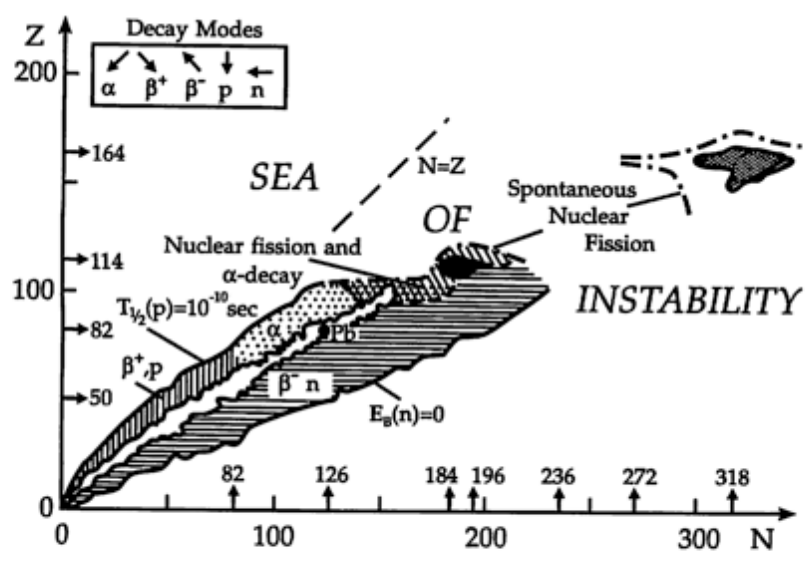


Fig. 1. The periodic system of elements as conceived by the Frankfurt school in the late sixties. The islands of superheavy elements ( $Z = 114$ ,  $N = 184$ ,  $196$  and  $Z = 164$ ,  $N = 318$ ) are shown as dark hatched areas.

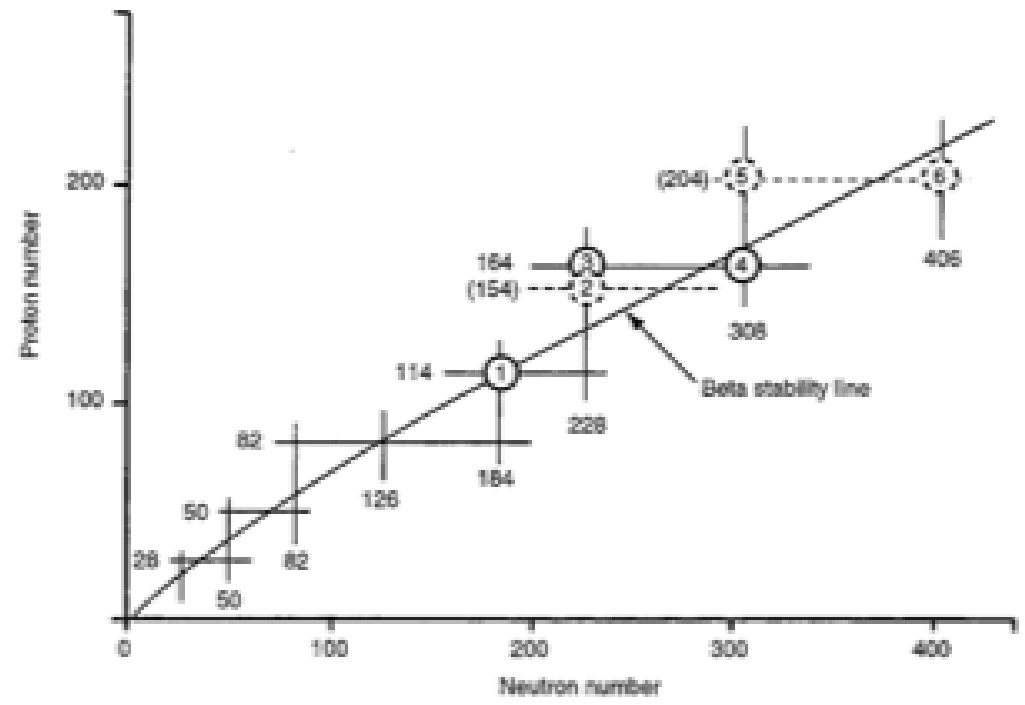


Figure 7.1 Calculated location of the islands of superheavy elements, 1, and super-heavy elements, 2-6, in the nuclear chart. The figure was taken from Sobiczewski (1974).

On Beyond Uranium, p.66 (S, Hofmann) 2002.  
Figure was taken from Sobiczewski (1974)

Lecture Notes in Physics 581, p.317 (Greiner) 2001  
*also in talks of Kratz and Greiner himself*

- ➔ **Some qualitative estimation were studied, but rather quantitative estimation are required.**
- ➔ **We estimate decay modes by using the KTUY mass formula.**

# KUTY(KTUY) mass formula

( Koura Uno, Tachibana, Yamada, (00), KTUY(05), PTP113, 305 )

$$M(Z, N) = M_{\text{gross}}(Z, N) + M_{\text{eo}}(Z, N) + E_{\text{sh}}(Z, N)$$

Mass table  
(Z,N>1, Z<131, N<201) :  
available from the web site of  
Nuclear Data Center of JAEA

$M_{\text{gross}}(Z, N)$ : Gross term

$A^{-1/3}$  expansion term including  $|N-Z|$ ,  $(N-Z)^2$  + **Coulomb term**

$E_{\text{sh}}(Z, N)$ : Shell term

**Spherical nuclei: Calculate from a modified Woods-Saxon potential (a function of Z, N) (NPA671(00)96)**

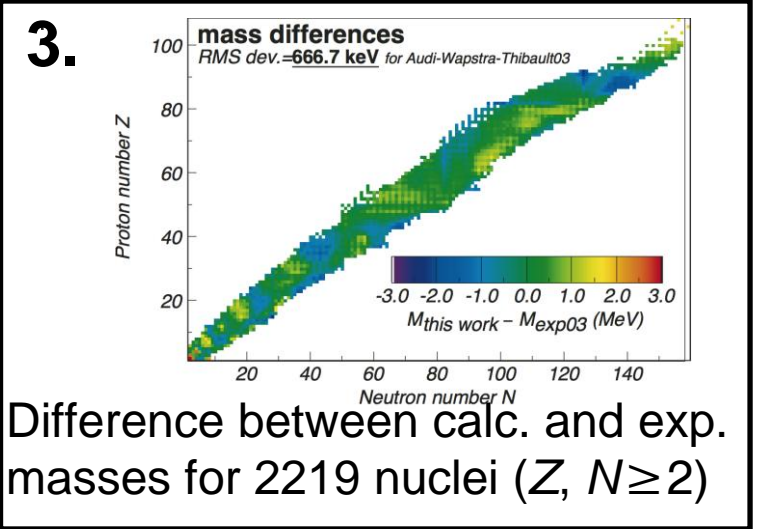
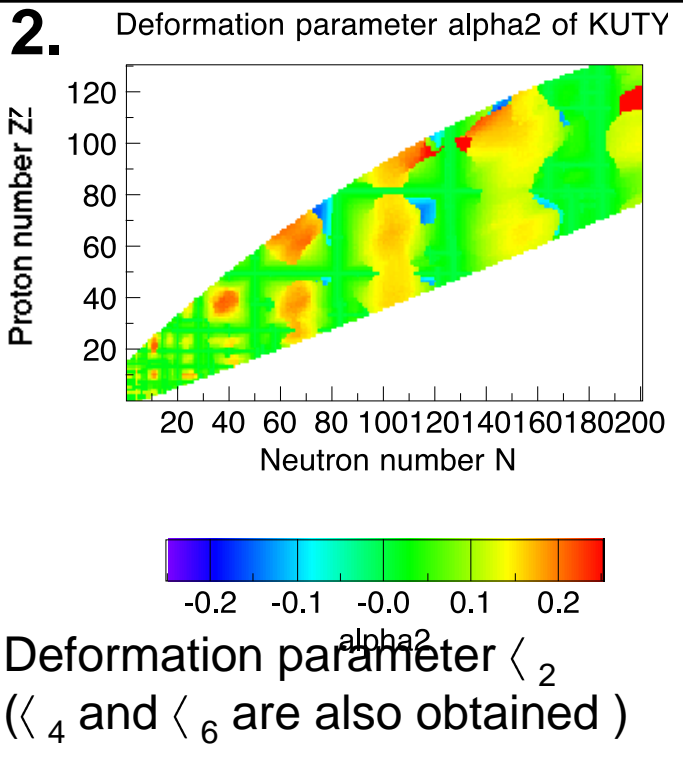
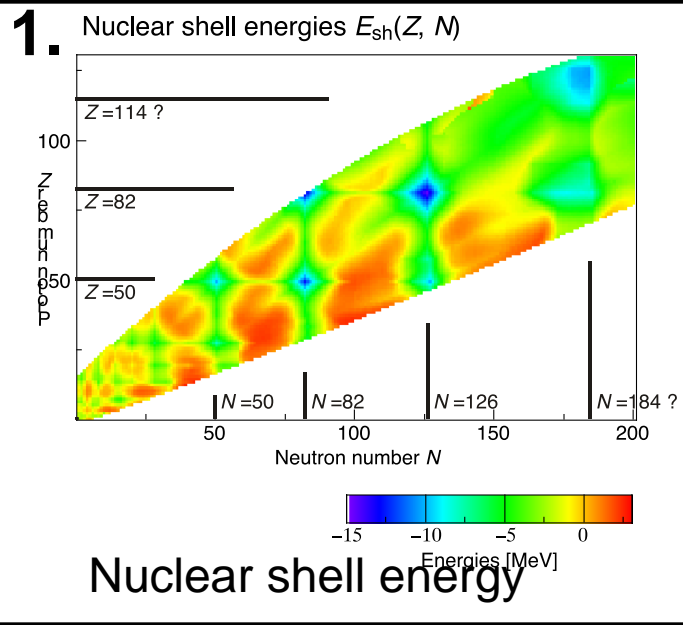
Spherical state of All nuclei are obtained.

**Deformed nuclei: Mixing weight of the above spherical shell energies weight : determined by shapes of nuclei (NPA674(00)47)**

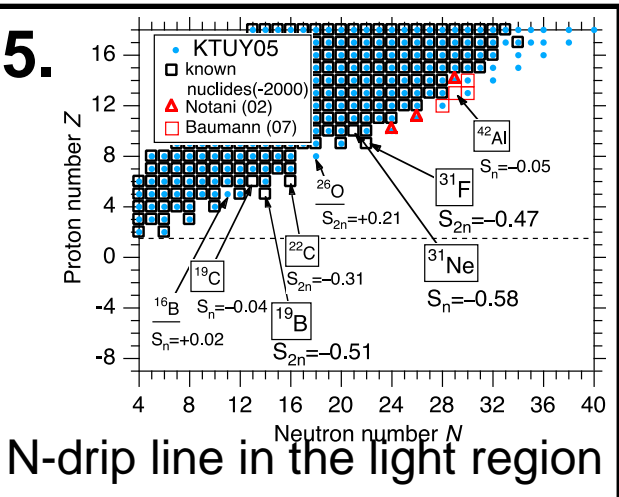
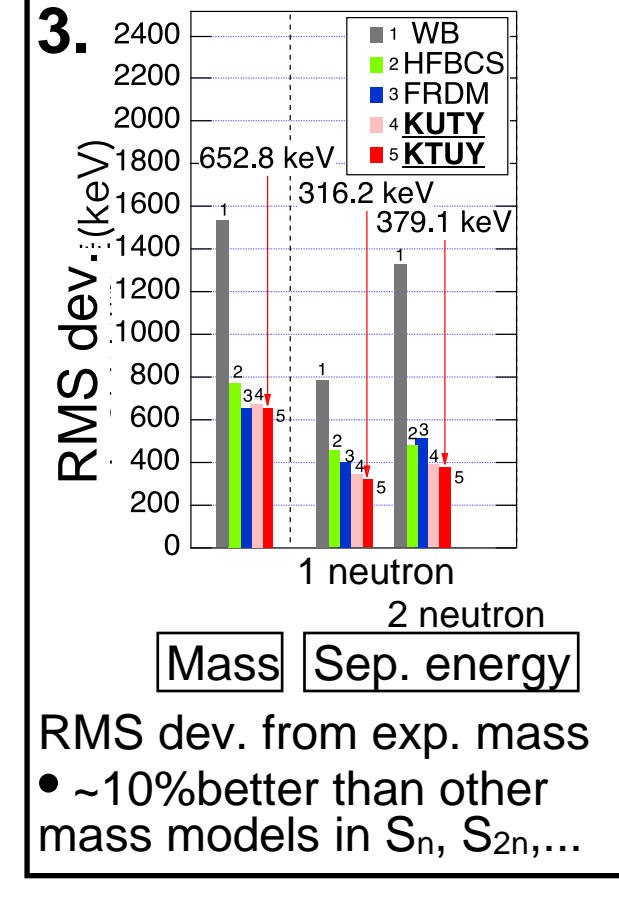
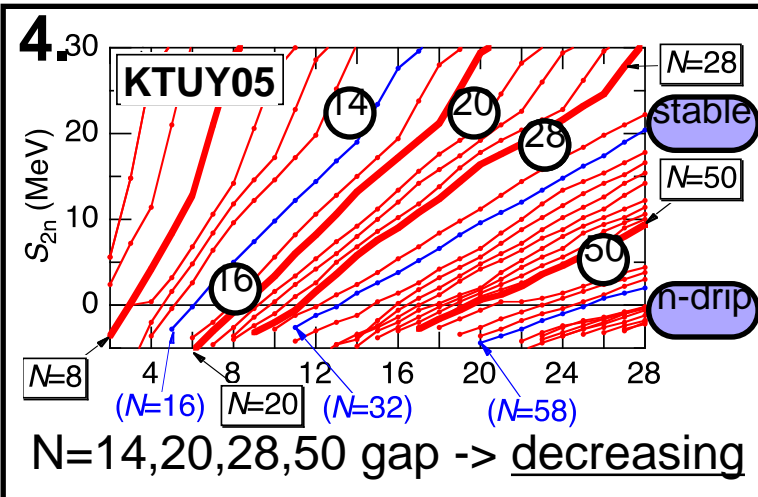
$$E_{\text{sh}}(Z, N) = \sum_{\text{def.}} (\langle E_{\text{sh}}^{\text{sph}}(Z, N) \rangle_{\text{def.}} + \Delta E_{\text{S}}(Z, N) - \Delta E_{\text{C}}(Z, N) - \Delta E_{\text{pro}}(Z, N))$$

*Micro*
*Surface*
*Coulomb*

# Results of the KTUY mass formula



1. Nuclear shell energy
2. Nuclear shape
3. better mass-reproduction
4. Change of magicities in n-rich
5. Reproduction of n-drip line
6. etc.



# Reproduction of the KTUY model

RMS deviation from experimental data in

keV

Mass formulas	Mass	Neutron	Proton	Alpha		Beta		
				$Q_\alpha$	$Q_\alpha > 0$	$Q_\beta$	$Q_{\beta^-} > 0$	$Q_{EC} > 0$
(n. of data)	(2149)	(1988)	(1948)	(1974)	(1860)	(1860)	(785)	(1073)
<b>KTUY</b>	<b>653</b>	<b>316</b>	<b>353</b>	<b>517</b>	<b>494</b>	<b>449</b>	<b>520</b>	<b>389</b>
FRDM	656	399	395	612	584	491	568	424
HBF2	659	470	490	550	521	581	636	541
HFB8	640	564	593	683	641	696	740	660

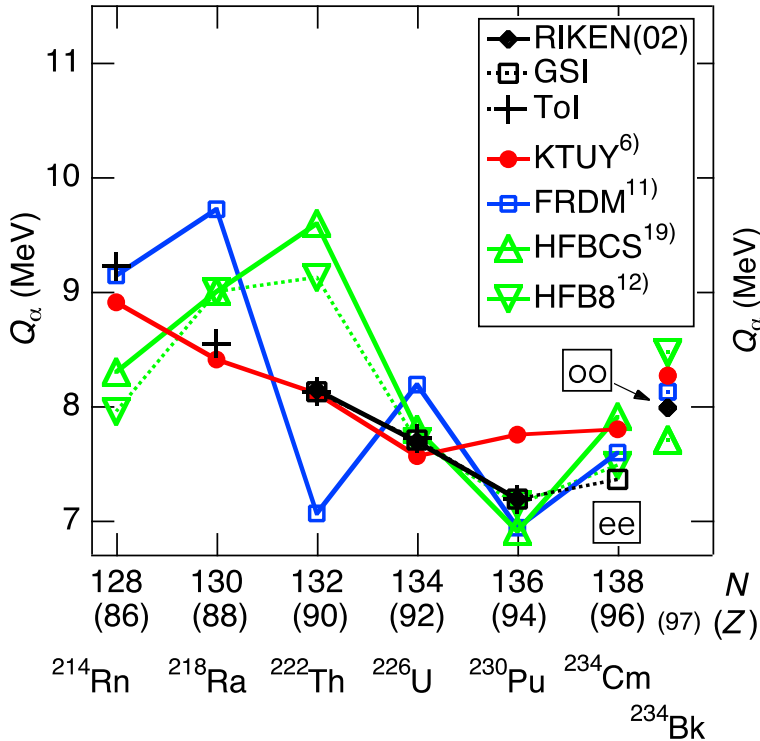
Exp. data: AME2003 by Audi et al.

- KTUY gives **Smallest RMS dev.** from exp. derivatives of masses by **10-20%**

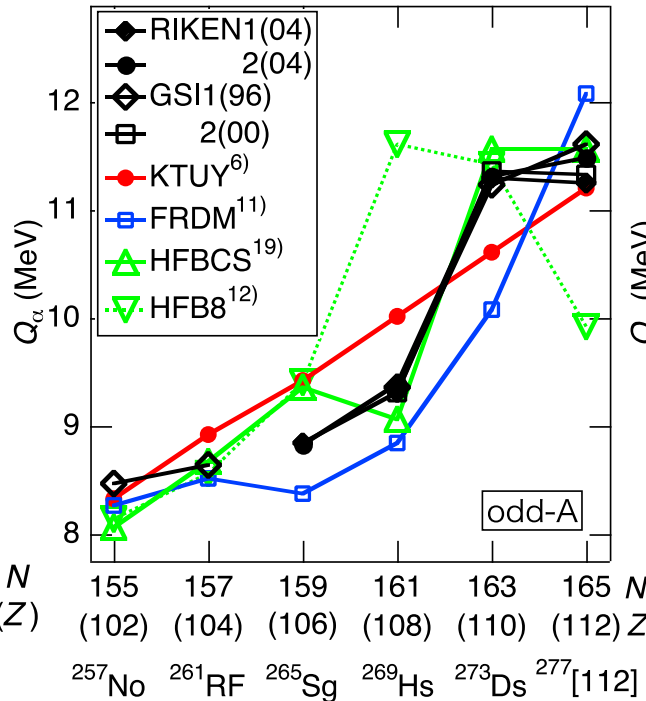


# $\alpha$ -decay Q-values from GSI and RIKEN

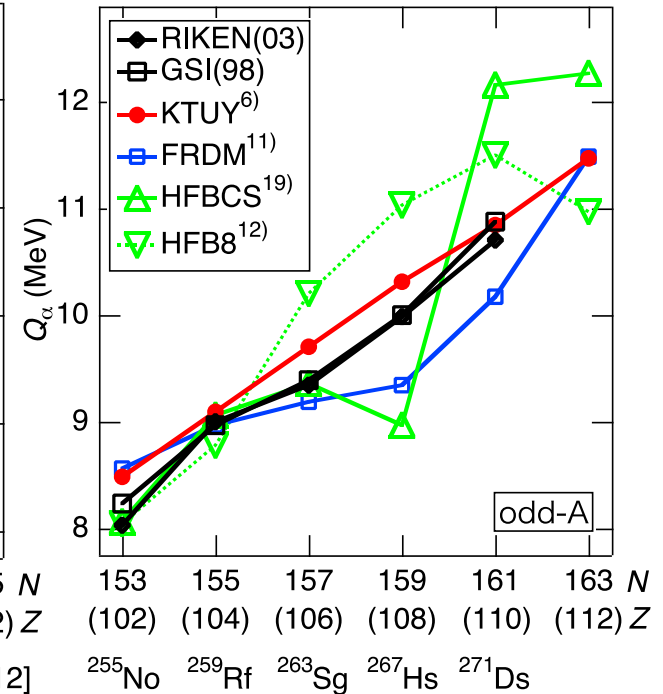
related to  $^{234}\text{Bk}$   $^{277}\text{Cn}$   $^{271}\text{Ds}$  ( $^{275}\text{Cn}$ )



Experiment: **smoothness**



Experiment: **steep at  $N \approx 162$ , flat at  $N \approx 164$**



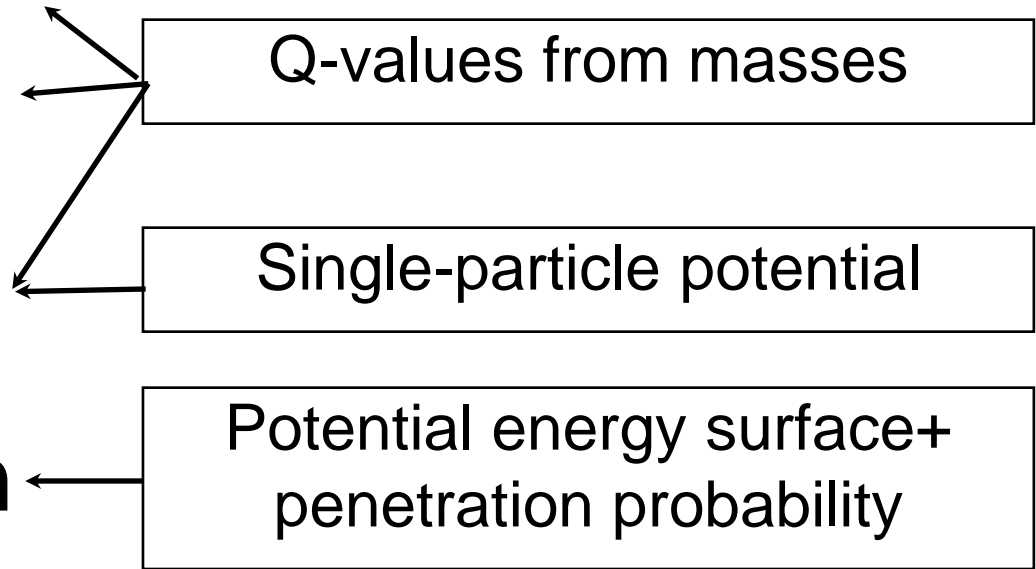
Experiment: **smoothness**

KTUY: smooth property, but deformed shell is not clear  
 \*All predictions are calculated as ground-to-ground-state

# Estimation of nuclear decay modes

- Alpha-decay
- Beta-decay
- Proton emission
- Spontaneous fission

## Sensitivity





# Alpha and beta decay half lives

Alpha decay: phenomenological relation between  $Q_\alpha$  and  $T_{\alpha 1/2}$ :

$$\log_{10} T_\alpha(\text{s}) = 1.7195 \sqrt{\frac{A-4}{A}} Z_D / \sqrt{Q_\alpha(\text{MeV})} - 1.2901 \sqrt{\frac{A-4}{A}} \sqrt{RZ_D} \\ + 0.07466 \sqrt{\frac{A-4}{A}} R^{3/2} / Z_D^{1/2} \cdot Q_\alpha(\text{MeV}) \\ - \log_{10} N - 0.159175 + h_0 \delta_{\text{eo}}.$$

$$R = r_0 A_D^{1/3} + d_0, \quad r_0 = 1.08 \text{ fm.}$$

- RMS dev.: **1/10~10 times** in partial half-lives if exp. Q-values are adopted.
- Uncertainty of estimated  $Q_\alpha$  is ~500 keV. Typically, shift of 300 keV gives a change of  $T_{1/2}$  in one order of magnitude in the superheavy mass region.
- Totally Uncertainty of  $10^{-3}$ - $10^3$  in  $T_{\alpha 1/2}$

Beta decay: the Gross theory of beta decay  $\lambda_F + \lambda_{\text{GT}} + \lambda_1^{(0)} + \lambda_1^{(1)} + \lambda_1^{(2)}$

$$\lambda_F = \frac{m_e^5 c^4}{2\pi^3 \hbar^7} |g_V|^2 \int_{-Q}^0 |M_F(E)|^2 f(-E) dE \quad \text{:Fermi (allowed)}$$

$$\lambda_1^{(2)} = \frac{m_e^5 c^4}{2\pi^3 \hbar^7} \left(\frac{m_e c}{\hbar}\right)^2 |g_A|^2 \int_{-Q}^0 \sum_{ij} |M_{ij}(E)|^2 f_1(-E) dE \quad \text{:1st forbidden}$$

$$|M_\Omega(E)|^2 \equiv \int_{\epsilon_{\min}}^{\epsilon_{\max}} D(E, \epsilon) W(E, \epsilon) \frac{dn_1}{d\epsilon} d\epsilon$$

$D(E, \epsilon)$  : One particle strength function

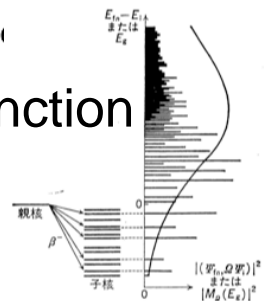
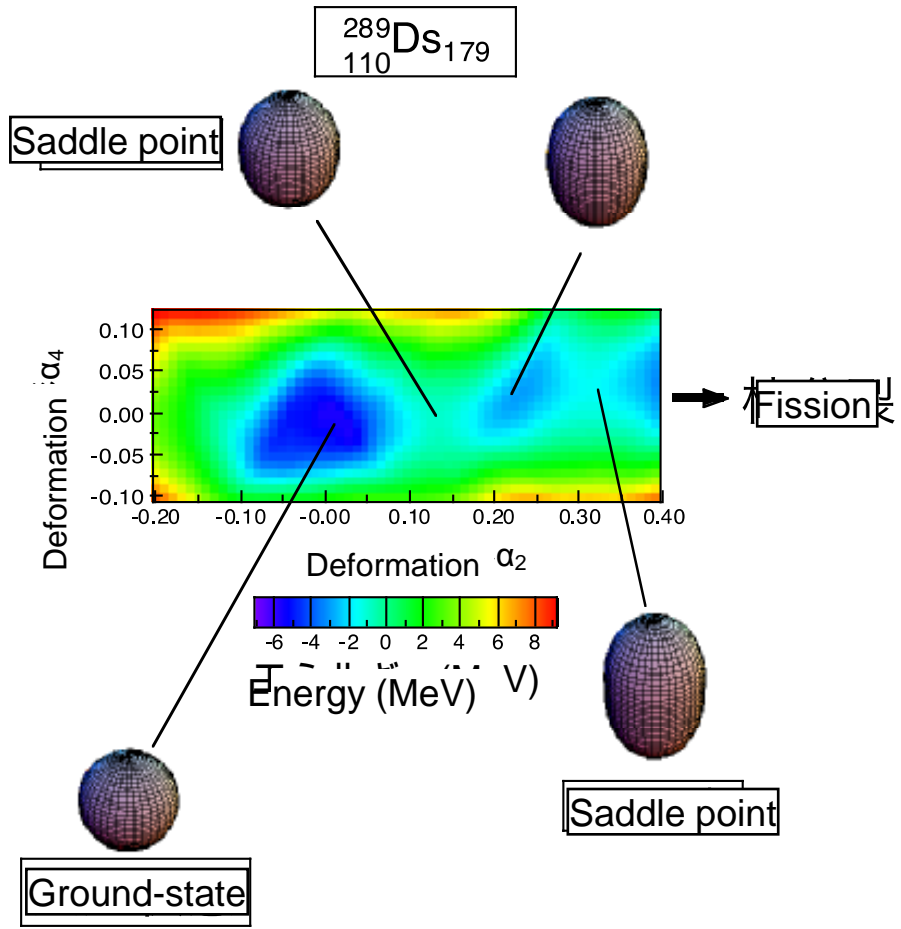


図 6・8 ベータ崩壊の強度関数の説明図

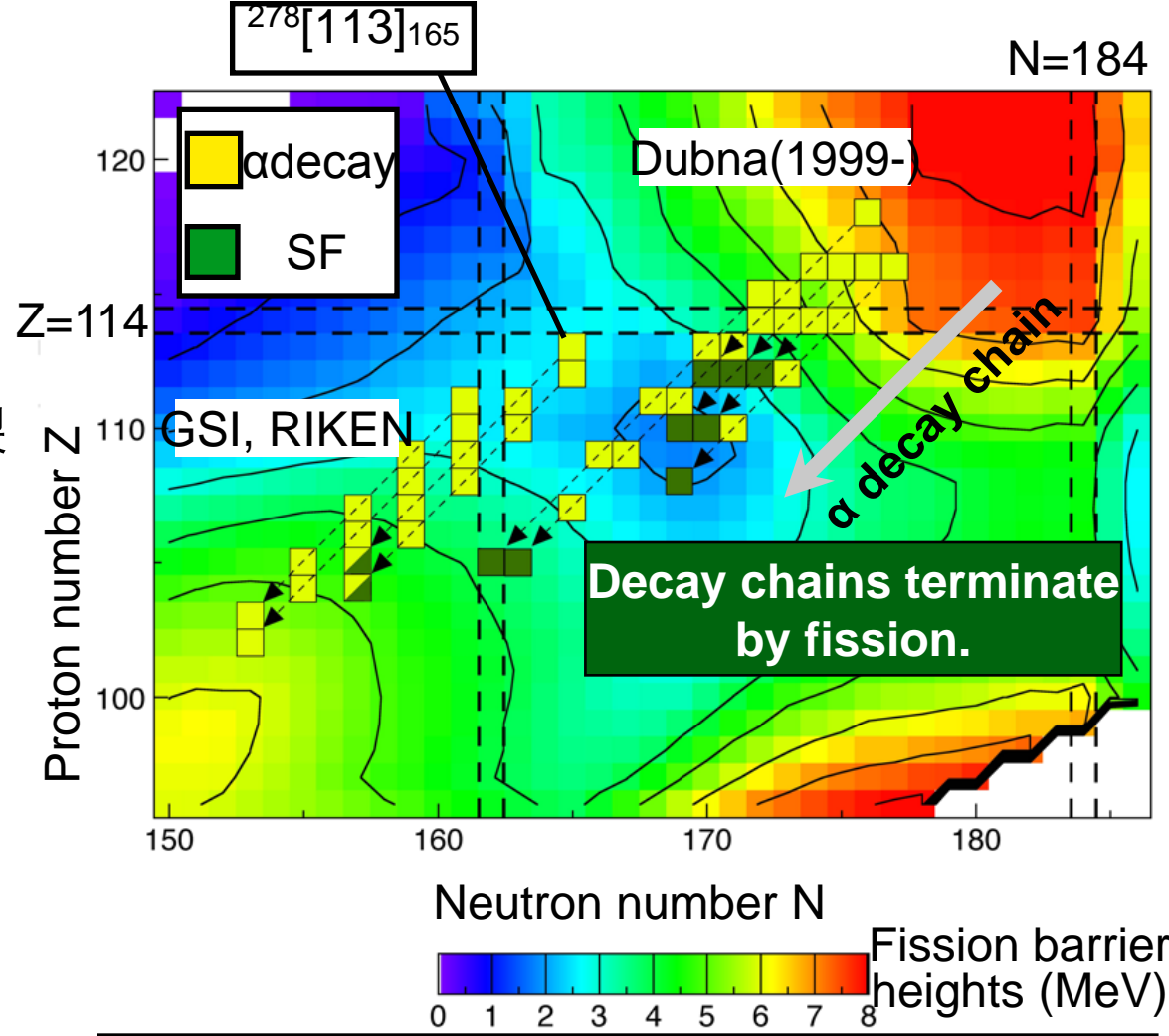
- Consider sum rules of beta-decay
- Not only allowed but also forbidden transition is treated:
- Averaged even-odd effect is introduced.

# Spontaneous Fission half-lives



Potential energy surface

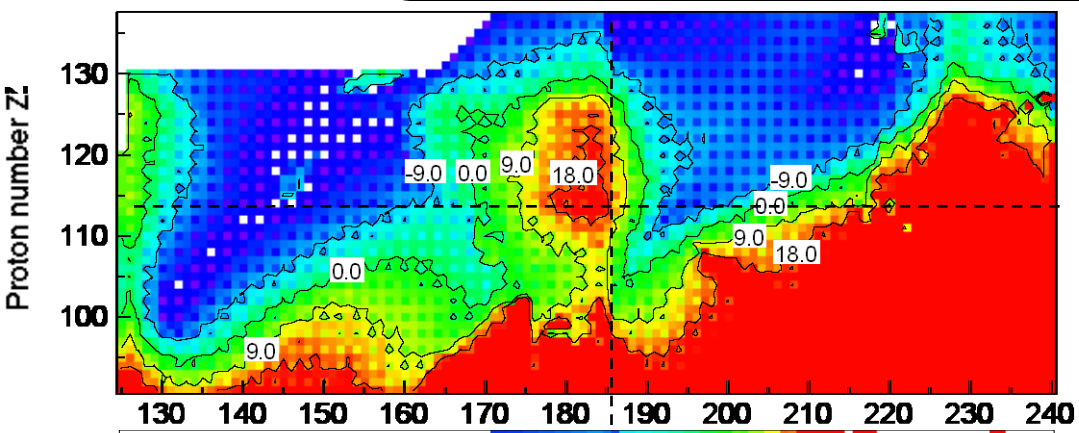
- Fission barrier height based on the KTUY mass calculation.



- SF-dominant region exists ( $N \approx 170$ ) (in agreement with measured data)

**Spontaneous fission half-lives:** Penetration probability is calculated with 1-dim. WKB method (mass inertia is adjustable parameter)

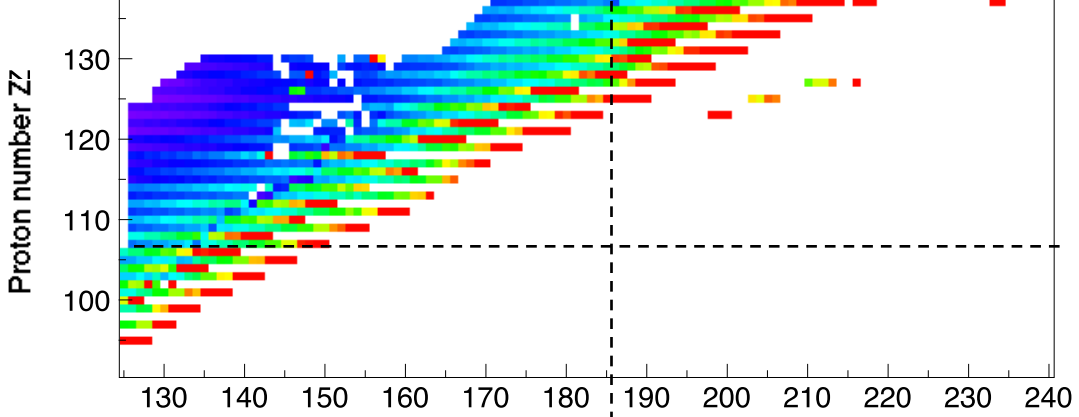
# Estimation of Partial half lives



Spontaneous fission

explained in previous page

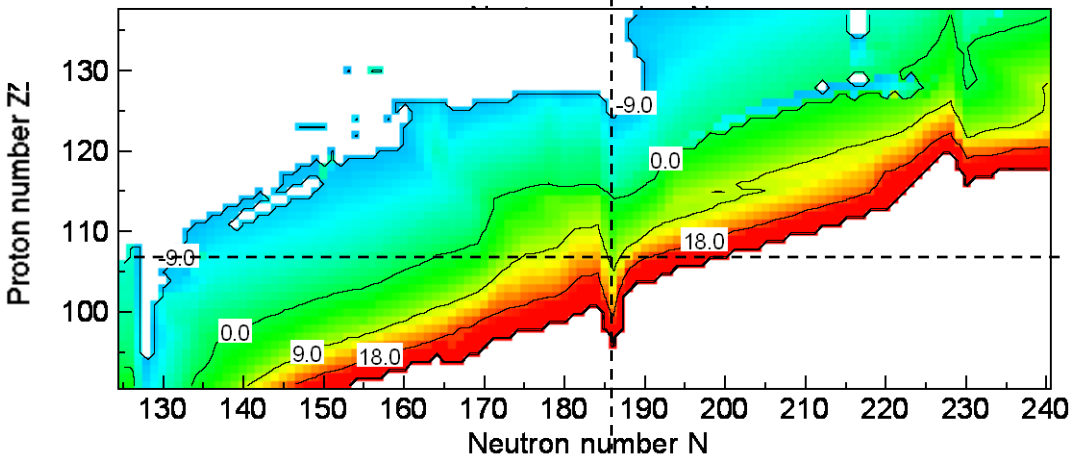
Quite sensitive to the shell closure.



Proton emission

WKB method  
 $Q_p, J^\pi$ : from **KTUY**

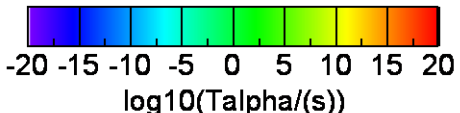
There has rather long partial half lives even outer proton-drip line



$\alpha$  decay

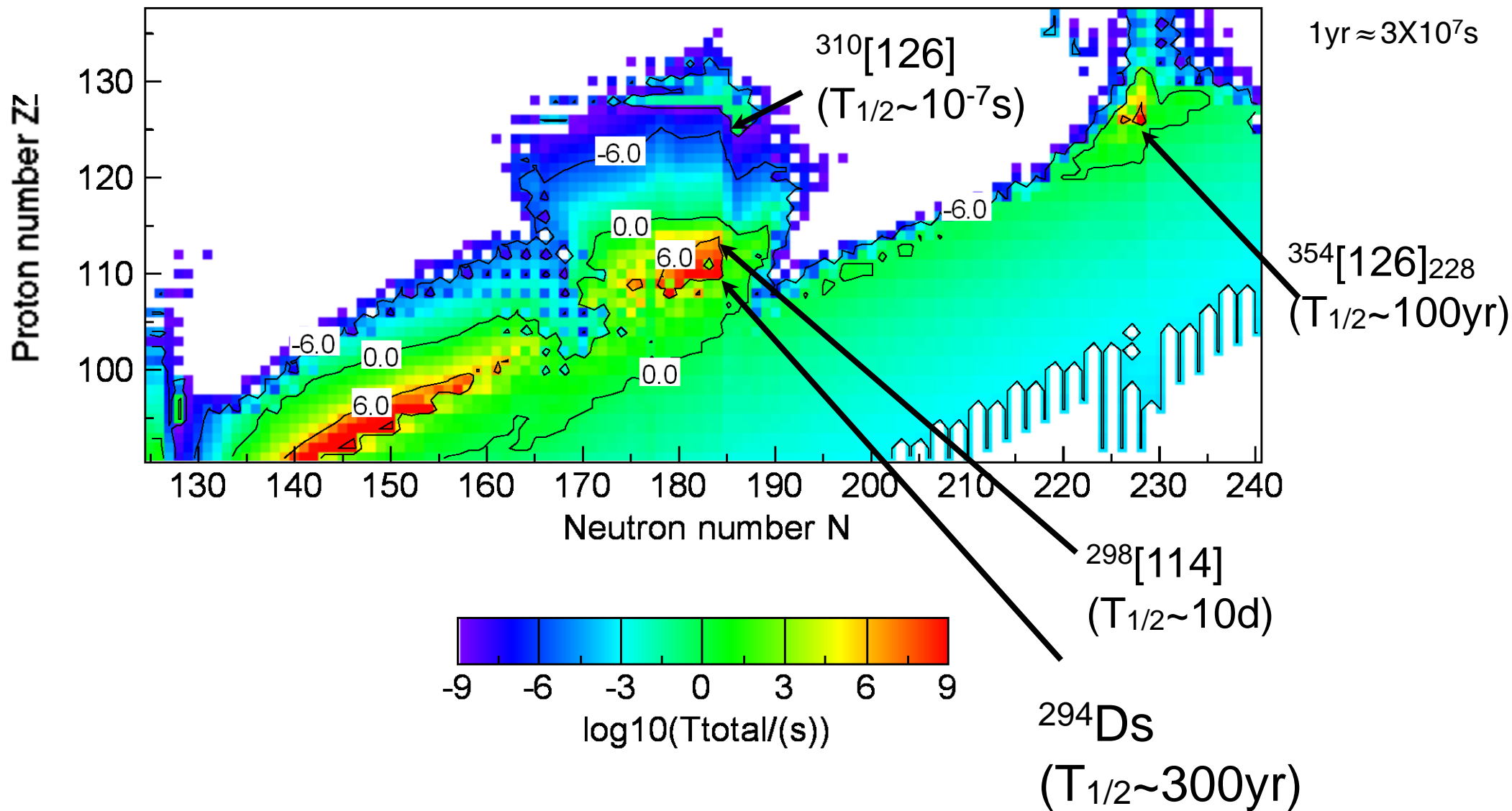
Phenom. formula  
 $Q_\alpha$ : from **KTUY**

Rather sensitive to the proton shell closure.



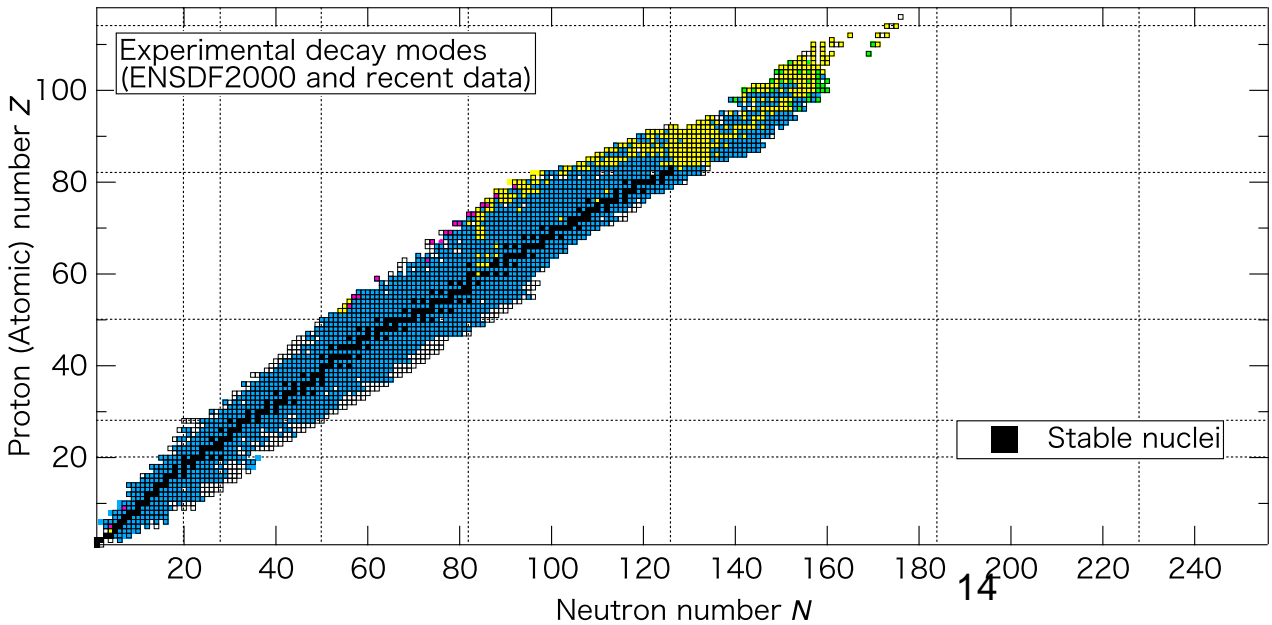
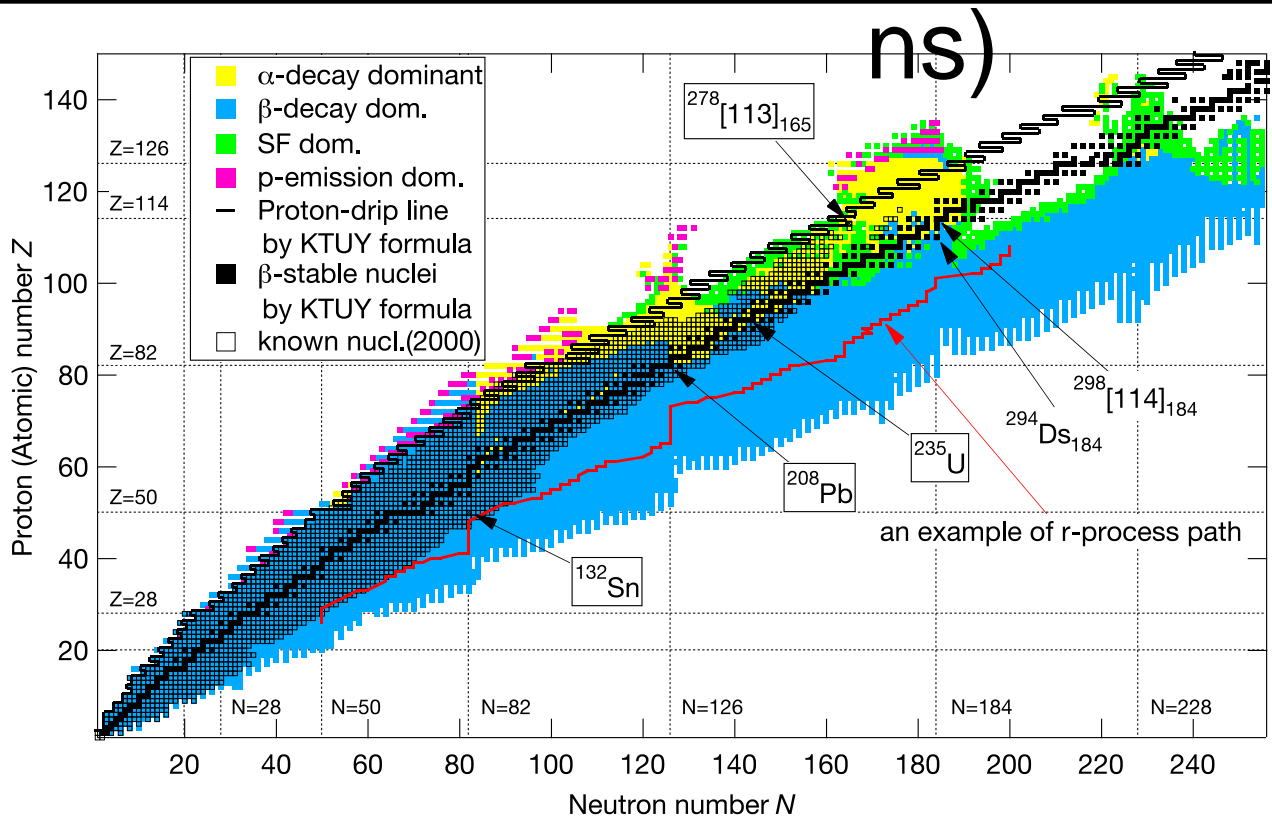
+  $\beta$ -decay by using the gross theory of  $\beta$ -decay + **KTUY**

# Total half-lives ( $\alpha, \beta, p, sf$ )



(Long-lived superheavy nuclei distributes near the  $\beta$ -stability line)

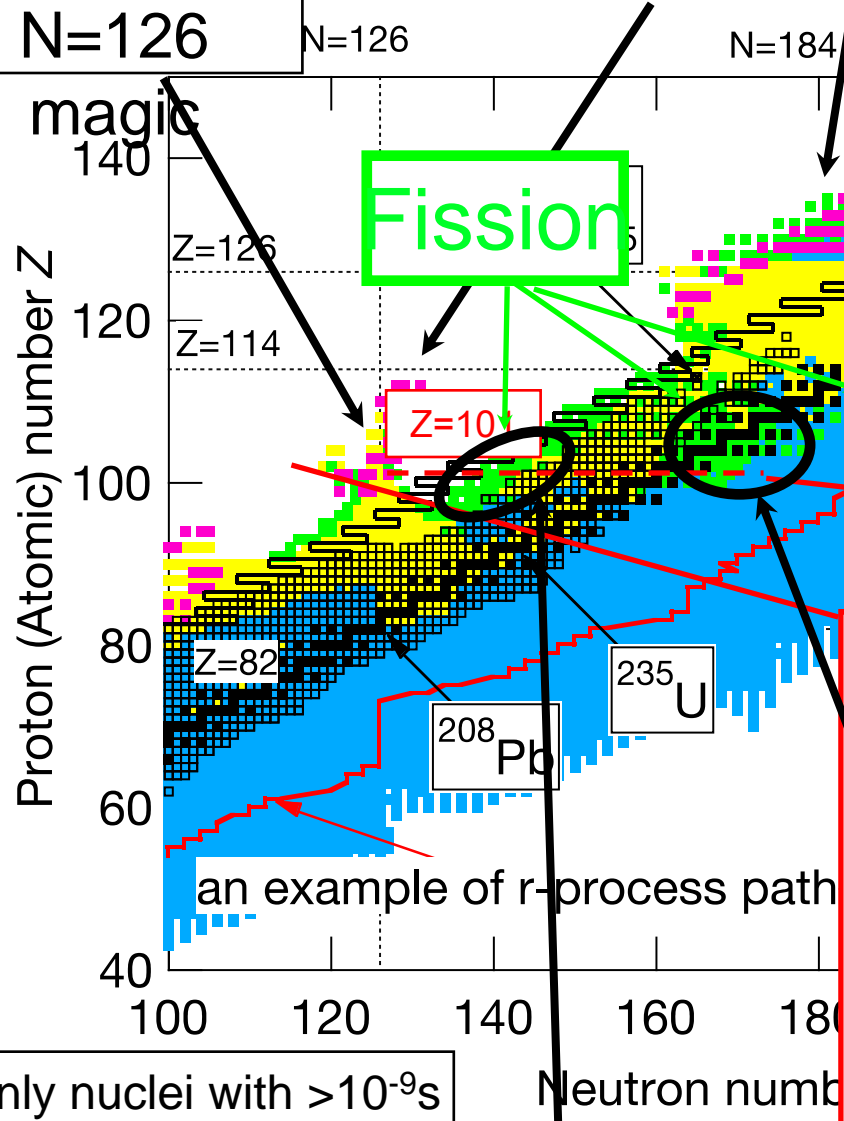
# Most dominant decay ( $\alpha$ , $\beta$ , sf, p) ( $T_{1/2} \geq 1$ ns)



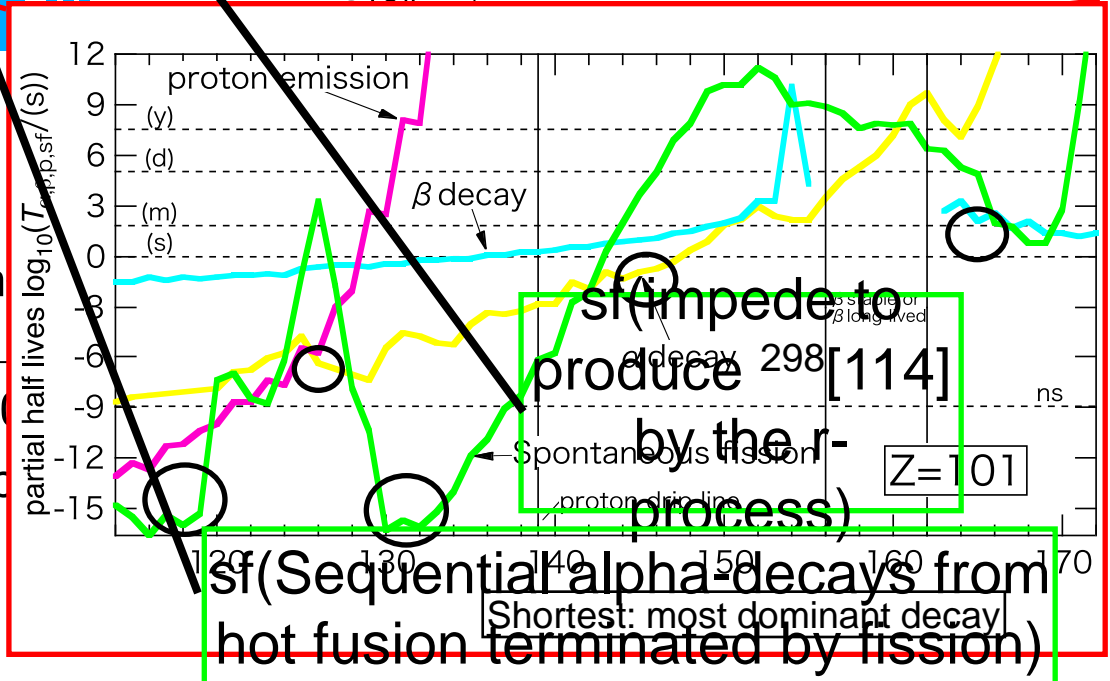
The bulletin of the Physical Society of Japan (BUTSURI), 60 (2005)

Periodicity of nuclear closed shell

"Cape"  
N=228 magic



How far does the area of nuclei extend? (finiteness)



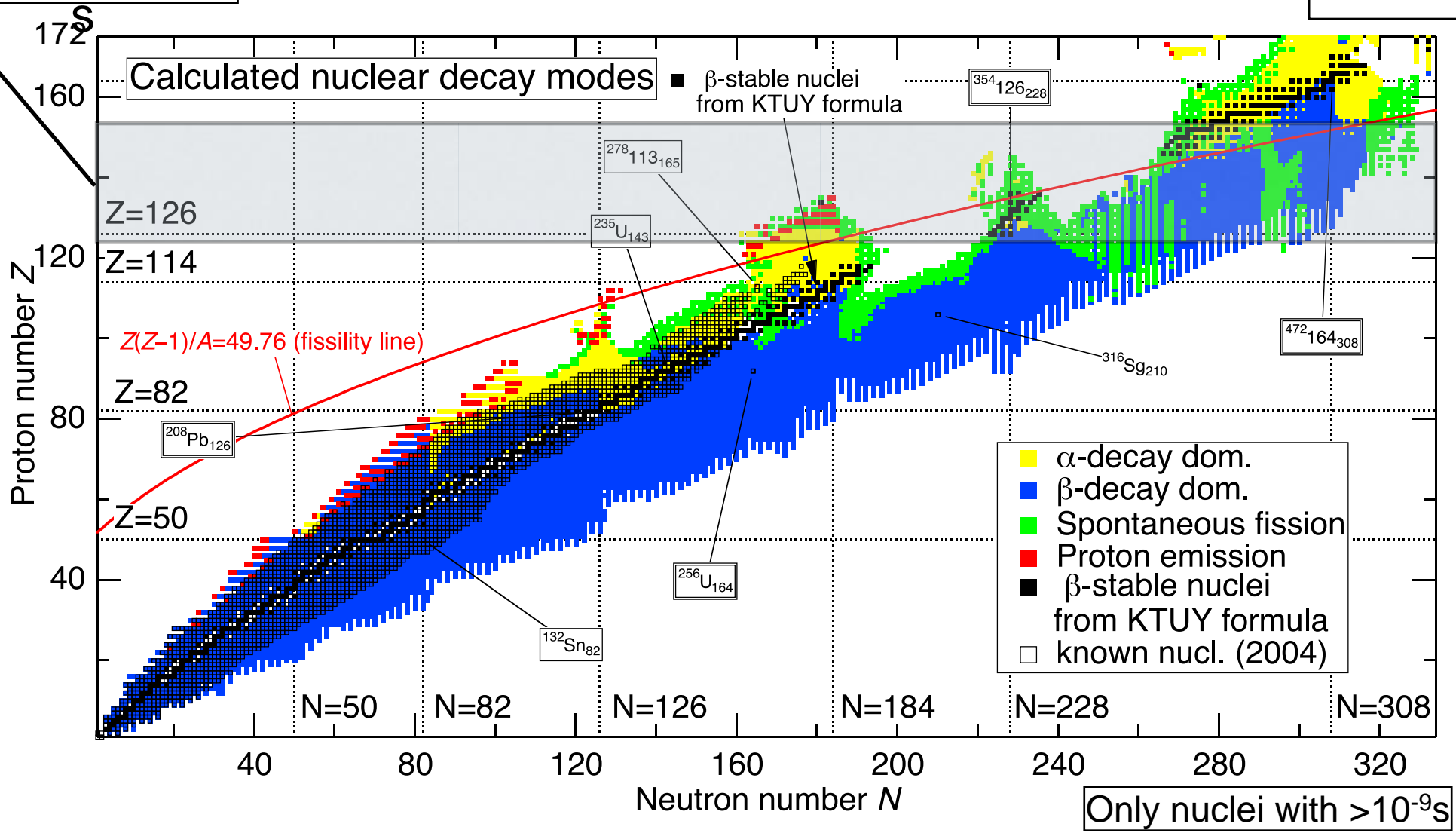
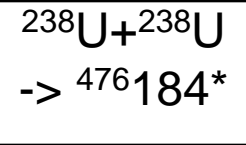
Only nuclei with  $>10^{-9}$ s

sf (more dom. than p)

sf (Sequential alpha-decays from hot fusion terminated by fission)

Superactinide

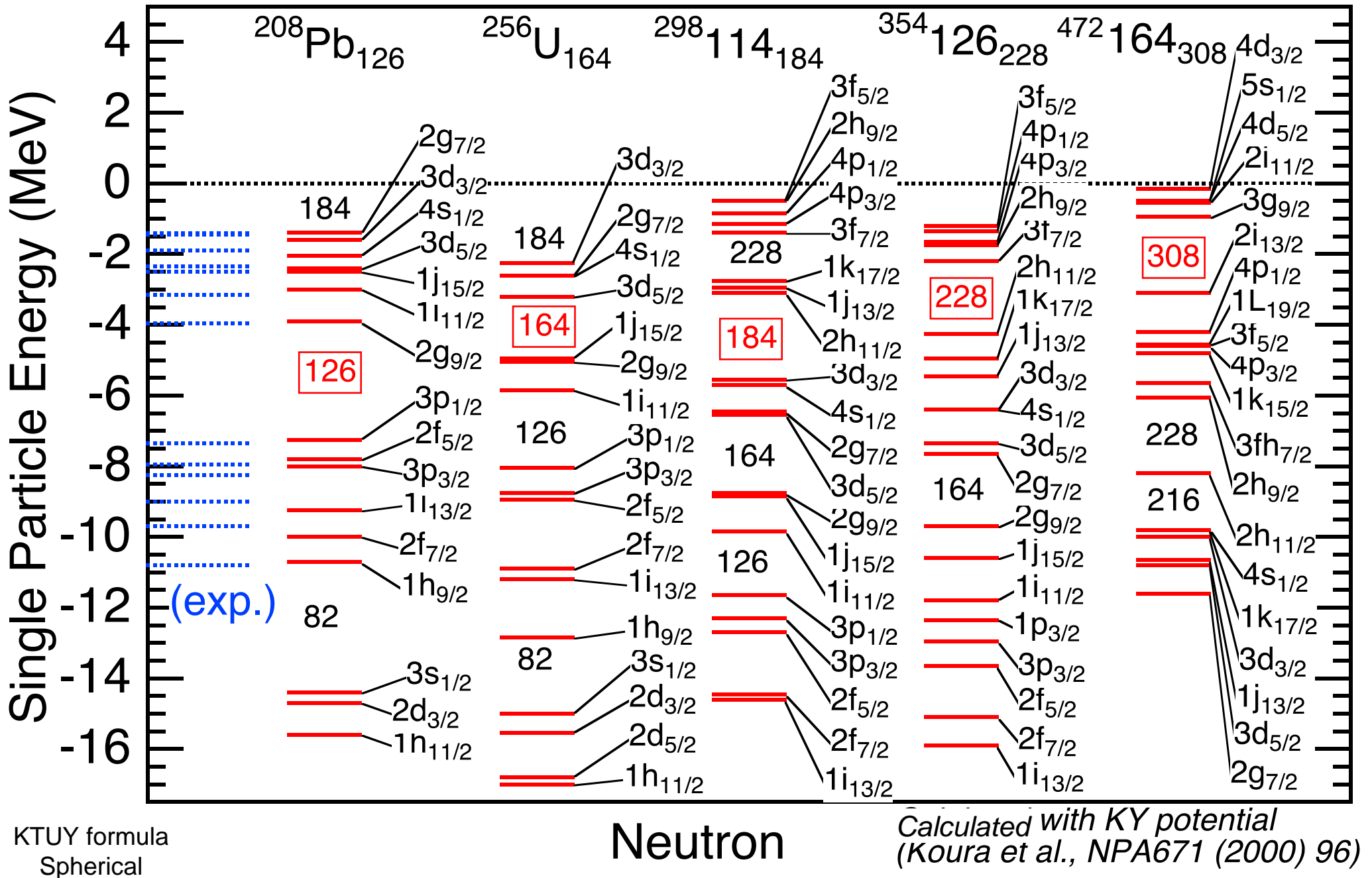
# Main decay modes



Spontaneous-fissioning nuclei is the border in the neutron-deficient side.  
 $T_{\text{sf}}=10^{-9}$  s line and neutron-drip line crosses near  $N \approx 340$ (cf. fissility line)  
 Islands of stability corresponding  $N = 228, 308, Z=164$  magicity appear.

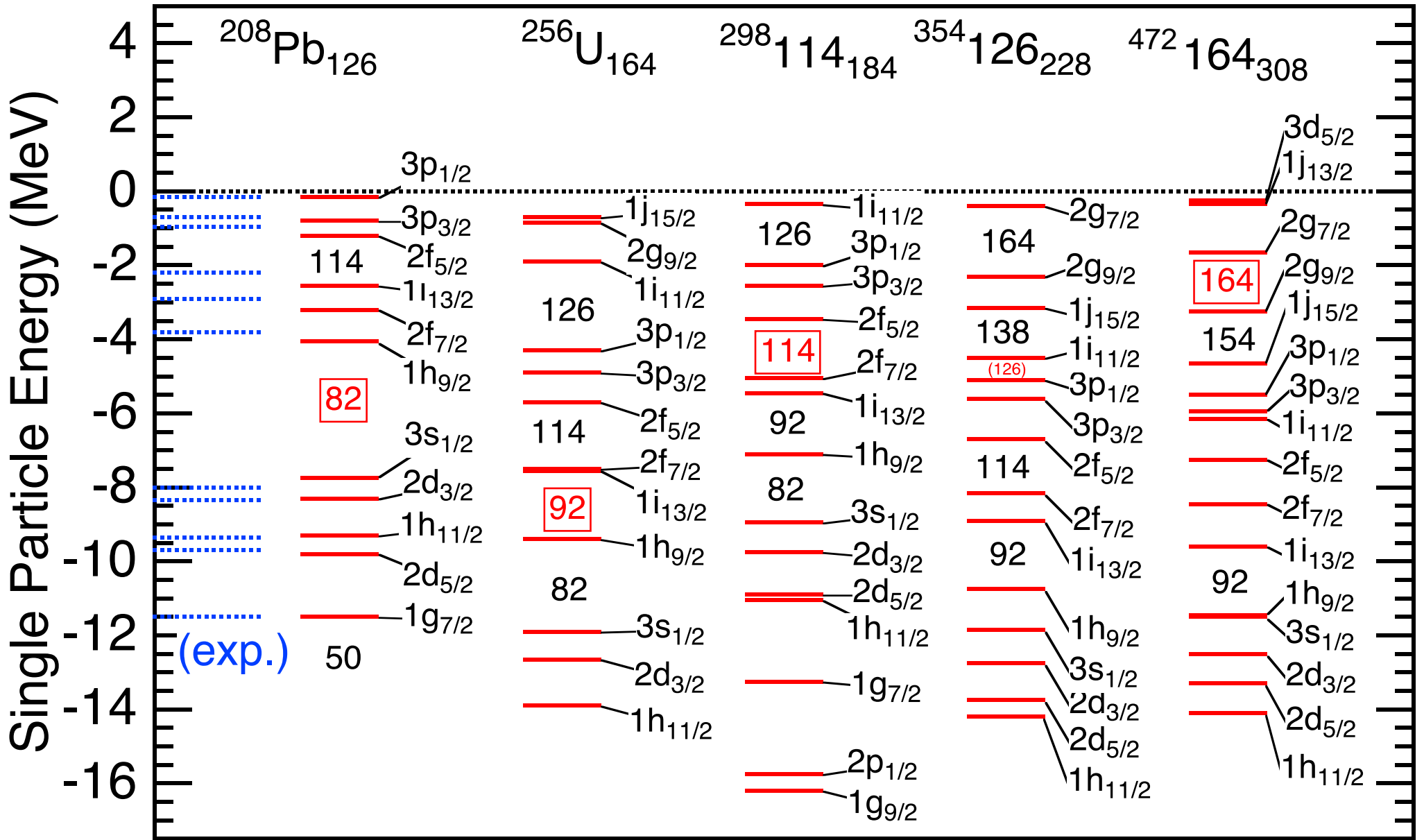


# Spherical neutron magic:beyond 184



Neutron: N=164, 184, 228, 308 gap appear clearly.

# Spherical proton magic: beyond 114 (or 126)

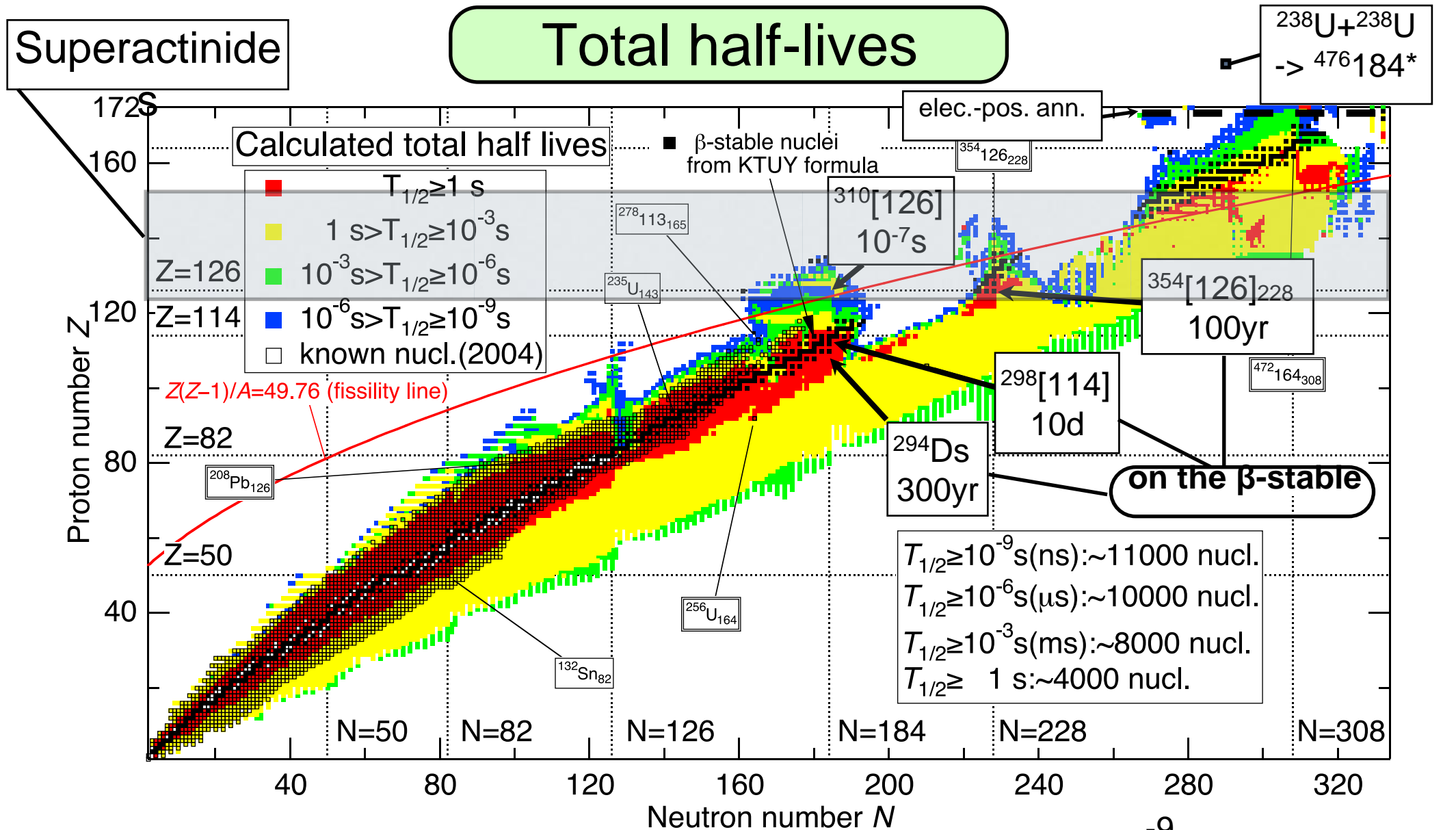


KTUY formula  
Spherical

Proton

Calculated with KY potential  
(Koura et al., NPA671 (2000) 96)

Proton: Z=114, 164 gap exist, but are no so remarkable.



Upper limit of Atomic number with half-lives longer than  $10^{-9} \text{ s}$ :

$N \approx 184 \text{ region} \Rightarrow Z \approx 136,$   
 $N \approx 228 \text{ region} \Rightarrow Z \approx 142,$   
 $N \approx 308 \text{ region} \Rightarrow Z \geq 175$

Uncertainty of half-lives : They may be in 3 order of magnitude. ex.  $^{294}\text{Ds}: 0.3 \text{ y} \sim 0.3 \text{ My}$

- We calculate nuclear decay modes and total half-lives in the (ultra) superheavy nuclear mass region by using the KTUY mass model.
- Nuclear decay mode of superheavy nuclei:
- **Other regions of “island of stability of superheavy nuclei”**
  - “Peninsula” near the proton-drip region along  $N=126$
  - Next “island (cape) of stability” along  $N=228$  (small) and also  $N=308$  (large) <- due to the shell closure of the nuclear mean-field potential.
- Limit of Existence of nuclei:
- **A finiteness of region of (relatively) long-lived nuclei**
  - Predicted number of nuclei:
    - 11,000 for nuclei with  $> 1$  ns
    - 10,000 for nuclei with  $> 1$   $\mu$ s
    - 8,000 for nuclei with  $> 1$  ms
    - 4,000 for nuclei with  $> 1$  s
  - Calculation region reaches the limit of macroscopic fissility line.

**Спасибо!**

**Thank you for your  
attention!**